## 淡江大學 96 學年度轉學生招生考試試題

46-1

系別: 化學工程與材料工程學系三年級 科目: 物 理 化 學

Problem One (15 points)

The wavefunction of an electron in the lowest energy state of a hydrogen atom is

PI

proportional to  $e^{-r/a_o}$ , with  $a_o$  a constant and r the distance from the nucleus.

Normalize the wavefunction.  $\int_0^\infty x^n e^{-ax} dx = \frac{n!}{a^{n+1}}$ 

Problem Two (30 points)

Some reactions proceed through the formation of an intermediate, as in the consecutive uni-molecular reactions

$$A \xrightarrow{k_a} I \xrightarrow{k_b} P$$

Each step of the reaction is first order. Derive the following relations:

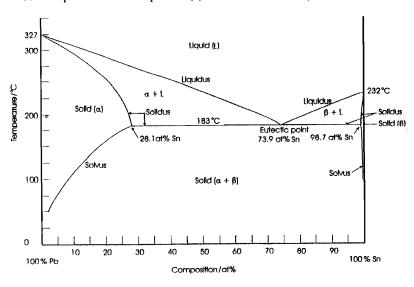
(a) 
$$[A] = [A]_0 e^{-k_{n'}}$$
,  $[A]_0$  is the initial concentration of A.

(b) 
$$[I] = \frac{k_a}{k_b - k_a} (e^{-k_a t} - e^{-k_b t}) [A]_0$$

(c) 
$$[P] = \left\{ 1 + \frac{k_a e^{-k_b t} - k_b e^{-k_a t}}{k_b - k_a} \right\} [A]_0$$

Problem Three (30 points)

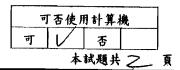
With respect to the lead-tin phase diagram shown below, the sample made up with 40 at% tin is cooled slowly to 250 °C. (a) What phases are present at 250 °C; (b) What is the composition of each phase? (c) How much of each phase is present?



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46-2

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Problem Four (25 points)

- (a) Calculate the change in entropy when 25 kJ of energy is transferred reversibly and isothermally as heat to a large block of iron at 100 °C.
- (b) Calculate the molar entropy of a constant-volume sample of neon at 500 K given that the entropy is  $146.22 \text{ JK}^{-1} \text{mol}^{-1}$  at 298 K.  $C_{p,m} = 20.786 \text{ JK}^{-1} \text{mol}^{-1}$
- (c) Calculate  $\Delta S$  (for the system) when the state of 3 mol of perfect gas atoms, for which  $C_{p,m}=\frac{5}{2}R$ , is changed from 25 °C and 1 atm to 125 °C and 5 atm.
- (d) Calculate  $\Delta H$  and  $\Delta S_{tot}$  when two copper blocks, each of mass 10 kg, one at 100 °C and the other at 0 °C, are placed in contact in an isolated container. The specific heat capacity of copper is 0.385 JK<sup>-1</sup>g<sup>-1</sup> and may be assumed constant over the temperature range involved.

10.

PZ