

# 淡江大學九十四學年度轉學生招生考試試題

系別：化學工程與材料工程學系三年級 科目：物理化學

准帶項目請打「V」

✓ 簡單型計算機

節次： 7 月 13 日第 3 節

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1. Evaluate the root mean square distance,  $\langle r^2 \rangle^{1/2}$ , of the electron from the nucleus in the hydrogen atom. The wavefunction of the electron is  $\Psi = \left(\frac{1}{\pi a_0^3}\right)^{1/2} e^{-r/a_0}$  where  $a_0 = 52.9$  pm. (Note that  $\int_0^\infty x^n e^{-ax} dx = \frac{n!}{a^{n+1}}$ .) 25%
2. Calculate the vibrational partition function at 50 °C for HCl molecules, which have the fairly high energy spacing of wave number 2885  $\text{cm}^{-1}$ . Given that  $q_{\text{vib}} = (1 - e^{-\Delta\epsilon_{\text{vib}}/kT})^{-1}$ . 25%
3. Three moles of an ideal mono-atomic gas is allowed to expand from an initial pressure of 200 bar to a final pressure of 5 bar, the temperature being maintained at 50°C. For the following three different processes, calculate  $\Delta U_{\text{therm}}$ ,  $\Delta U_{\text{mech}}$ ,  $\Delta U$ , and  $\Delta H$ .
  - (a) reversible expansion 10%
  - (b) irreversible expansion against a piston that maintains a force equal to a pressure of 5 bar 15%
4. Prove the following relation:  $\left(\frac{\partial H}{\partial p}\right)_T = V - T\left(\frac{\partial V}{\partial T}\right)_p$ . 25%