

淡江大學104學年度日間部轉學生招生考試試題

系別：運管系、統計系二年級

科目：微積分

考試日期：7月25日（星期六）第1節

本試題共7大題，1頁

注意事項：(1) 請按題號順序作答，並註明題號。(2) 可用鉛筆。(3) 不可使用計算機。(4) 需要計算過程。

1. (10%) (a) Find the limit $\lim_{x \rightarrow 1} \frac{x^2 - 1}{|x - 1|}$ if it exists. (b) If $\lim_{x \rightarrow -2} \frac{f(x)}{x^2} = 1$, find $\lim_{x \rightarrow -2} \frac{f(x)}{x}$.
2. (20%) (a) Find $f'(x)$ if $f(x) = \frac{1 + \ln x}{1 - \ln x}$. (b) Find dy/dx : $\sqrt{x+y} = 1 + x^2y^2$.
3. (15%) Determine where the function $f(x) = \frac{x^2}{x^2 + 3}$ is increasing and decreasing, and where its graph is concave up and concave down. Find the relative extrema, inflection points and asymptotes. Sketch the graph of the function.
4. (20%) Find the integral. (a) $\int \ln x \, dx$. (b) $\int \frac{1}{x^2} \left(\frac{1}{x} - 1\right)^{2/3} \, dx$.
5. (10分) Determine whether the integral $\int_{-\infty}^{\infty} xe^{-2x^2} \, dx$ is convergent or divergent. Evaluate it if it is convergent.
6. (10%) Find the average value of $f(x, y) = xy$ over the given region D , where D is the triangle with vertices $(0, 0)$, $(1, 0)$ and $(1, 3)$.
7. (15%) Find the maximum and minimum values of $f(x, y) = e^{xy}$ subject to $x^2 + y^2 = 4$.