

淡江大學 100 學年度碩士班招生考試試題

53-1

系別：電機工程學系控制系統組
電機工程學系機器人工程所

科目：控 制 系 統

考試日期：2月28日(星期一) 第2節

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1. Find a state space representation for the transfer function

$$G(s) = \left[\begin{array}{c|c} \frac{-(12s+6)}{3s+34} & \frac{22s+23}{3s+34} \end{array} \right]. \quad (10\%)$$

2. Consider the control system shown in Fig. 1. The plant dynamics are described by the transfer

function $G(s) = \frac{1}{s^2 + 3s + 2}$ If we assume a unity-feedback control system with a PID

control $D(s) = K(1 + 2s + T_I / s)$

(i) Find the range of K for which this system is stable when $T_I = 5$. (10%)

(ii) With no integral control, i.e., $T_I = 0$ find a sufficient value for the gain K so that the poles $s_{1,2}$ of the closed loop system have $\text{Re}(s_{1,2}) < -0.5$ and $|\text{Im}(s_{1,2})| < 2$ (10%)

3. An open-loop mechanical system is governed by the second order system $\ddot{y} + 6\dot{y} + 5y = u(t)$, where $u(t)$ is considered the input and $y(t)$ is the output state.

(i) Take the Laplace transform (with zero initial conditions) to determine the open-loop transfer function between $U(s)$ and $Y(s)$. (10%)

(ii) Is the open-loop system stable? (10%)

(iii) Design a feedback control system with variable gain K which will remove the steady-state error when the system is subjected to a unit step input. (10%)

(iv) For what values of K is the closed-loop system stable? (10%)

4. For the electrical circuit shown in Fig. 2, find the transfer function from $u(t)$ to $y(t)$. (10%)

5. Consider a robot manipulator described by Fig. 3. If gravity and friction are ignored the system has the dynamics

$$(J + ML^2)\ddot{\theta} = T(t), \quad (1)$$

where θ is angular displacement, T is motor torque, $J = 1$, $M = 8$, and $L = 2$. To improve the performance we consider using the proportional-derivative controller

$$T(s) = K(\theta_r - \theta) - K_v \dot{\theta}(s), \quad (2)$$

where K and K_v are the proportional and derivative gains respectively.

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- (i) Draw a unity feedback block diagram (not simplified) described by Eq. (1) and (2). (10%)
- (ii) Use the block diagram to find the transfer function $G(s) = \frac{\theta}{\theta_r}$ (10%)

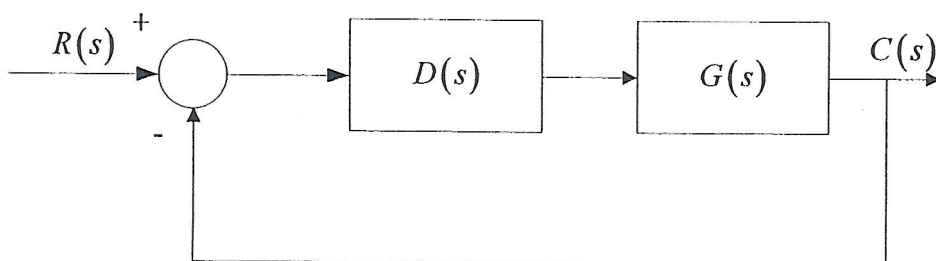


Figure 1

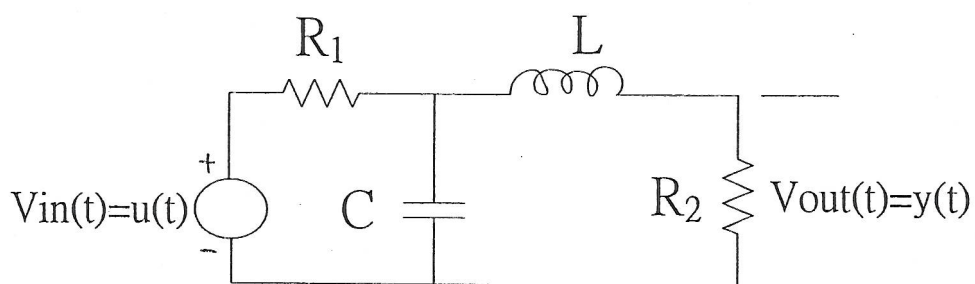


Figure 2

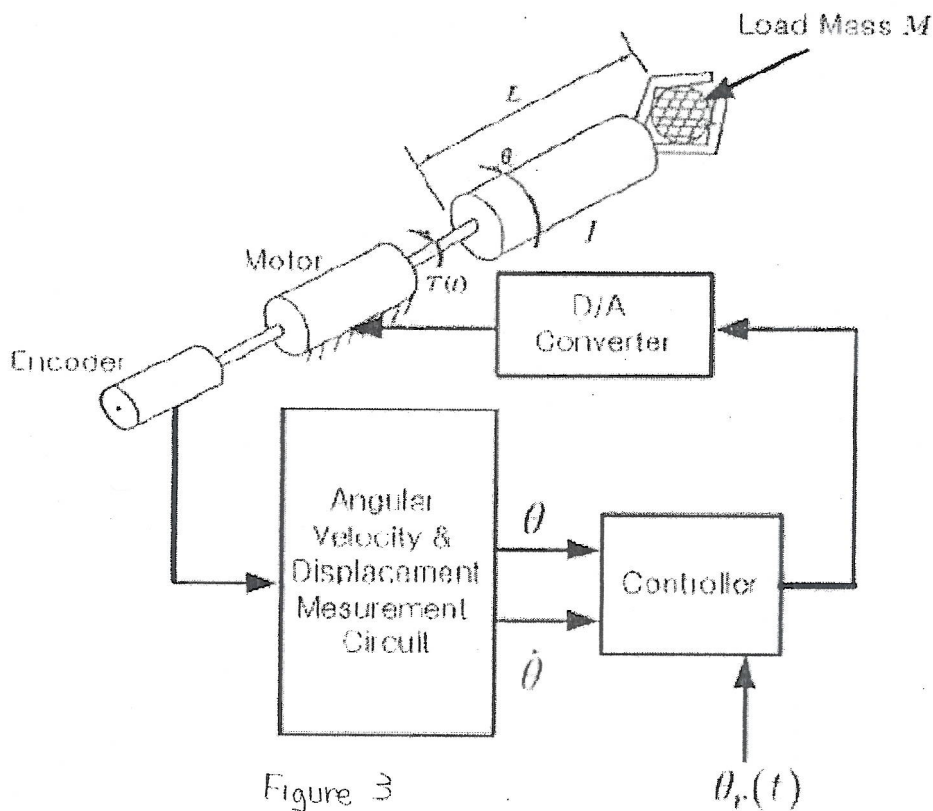


Figure 3