

淡江大學八十七學年度碩士班入學考試試題

系別：電機工程學系

科目：電磁學(含電磁波)

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I. A charge distribution with spherical symmetry has density

$$\rho = \begin{cases} \frac{\rho_0 r}{R} & , 0 \leq r \leq R \\ 0 & , r > R \end{cases} \quad (20\%)$$

determine potential  $V$  everywhere and the energy stored in region  $r < R$ .

II. Two conducting cones ( $\theta = \frac{\pi}{10}$  and  $\theta = \frac{\pi}{6}$ ) of infinite extent are separated by an infinitesimal gap at  $r=0$ . If potential  $V(\theta = \frac{\pi}{10}) = 0$  and  $V(\theta = \frac{\pi}{6}) = 50V$ , Find  $V$  and electric field  $\vec{E}$  between the cones.

(20%)

III. Determine the inductance per unit length for a two wire transmission line with separation distance  $d$ . The radius of each wire is  $a$ .

(20%)

IV. The plane wave  $\vec{E} = 50 \sin(\omega t - 5x) \hat{a}_y$  V/m in a lossless medium

( $\mu = 4\mu_0$ ,  $\epsilon = \epsilon_0$ ) encounters a lossy medium ( $\mu = \mu_0$ ,  $\epsilon = 4\epsilon_0$

$\sigma = 0.1$  mhos/m) normal to the  $x$ -axis at  $x=0$ , find the reflected

and transmitted  $\vec{E}$  and  $\vec{H}$  fields. (20%)

V. For the two short-dipole antenna array as shown in the figure, write down and sketch the normalized field pattern when the current are fed  $90^\circ$  out of phase and  $d = (\frac{1}{4}$  wavelength). (20%)

