

系別：航空太空工程學系

科目：自動控制

考試日期：2月26日(星期日) 第2節

本試題共 五大題， 2 頁

本試題雙面印刷

1. (30%) Consider the linear system shown in Figure 1 with transfer function

$$H(s) = \frac{-2s + 2K}{K(s+1)(s+2)}$$

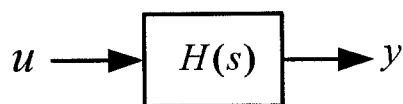


Figure 1.

where K is a scalar variable. This structure allows us to study the effects of a variable zero location, without affecting the location of the poles and the D.C. gain of the system.

(a). Find the step response of the system, i.e., determine $y(t)$ when $u(t)$ is a unit step function.

(Hint: Use partial fraction expansion to express the step response in the form

$$y(t) = \frac{a}{s} + \frac{b}{s+1} + \frac{c}{s+2}, \text{ express } a, b, \text{ and } c \text{ in terms of } K) \quad (10\%)$$

(b). Sketch the step responses of the system for $K = -10, -0.2, -1, -2, 0.2,$ and 10 respectively. (10%)

(c). From the results in (b), comment the impact on the transient response for different zero locations. (Note: discuss the effect of slow, fast, stable, and unstable zeros) (10%)

2. (20%). A unity feedback control system is shown in Figure 2 below. The transfer function of the open loop system is

$$P(s) = \frac{K_m}{s(Js + B)}$$

The parameters of the system are $J = 100, B = 140, K_m = 500$. The control gain K is to be determined to satisfy certain performance requirement.

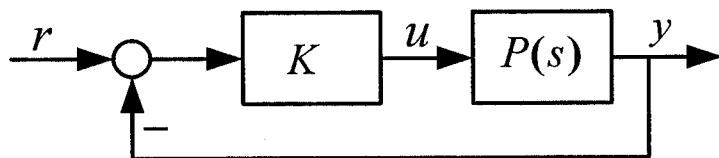


Figure 2.

(a). Find the range of values of the control gain K which ensure that the closed-loop system has a damping ration $\zeta \geq 0.7$. (10%)

(b). If the reference input is a unit ramp function, $r(t) = t, (t \geq 0)$, find the minimum steady state error which can be attained such that $\zeta \geq 0.7$. (10%)

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3. (20%) Consider the unity feedback control system shown in Figure 3 with

$$P(s) = \frac{1}{(s-1)(s+2)} \quad ; \quad K(s) = 4 \frac{s+\alpha}{s}$$

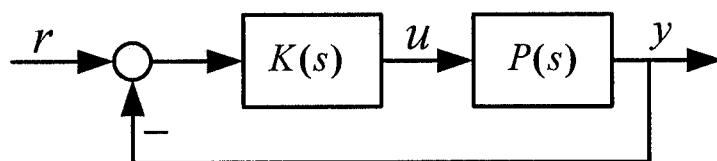


Figure 3.

Plot the root locus of the closed-loop system poles using α as the variable.

- On the root locus, show where $\alpha = 0$, and $\alpha \rightarrow \infty$. Show the direction of travel of the roots. (5%)
 - Find any asymptotes, centroids, and breakaway points. (5%)
 - Find the intersection of the root locus with the imaginary axis. (5%)
 - For what range of α is the closed-loop system stable. (5%)
4. (20%) Proportional plus integral controller (PI controller) is widely used in industrial process. Answer the following questions.
- What is a PI controller? Write its input-output transfer function. (6%)
 - What are the effects of the PI controller on the steady-state error of the system? Does the PI control change the system type? (6%)
 - What are the advantages and disadvantages of a properly designed PI controller for the control system. (8%)
5. (10%) State the general form and characteristic of a phase-lead compensator. What are the general effects of incorporating a lead compensator into a control system?