

系別：水資源及環境工程學系

科目：工程數學

准帶項目請打「V」

簡單型計算機

本試題共 / 頁

1. Solving $2(e^x \cos y + 1)y' - 4x + 2e^x \sin y = 0$

(20%)

2. Determining $\mathcal{L}[f]$ if $f(t) = 0$ for $0 \leq t < 2$
and $f(t) = 1 + t^2$ for $t \geq 2$

(20%)

3. Finding the function $y(x)$ that passes through the points $(0, 0)$ and $(1, 1)$ and minimizes $J[y] = \int_0^1 [y^2 + y'^2] dx$

(20%)

4. Solving partial Differential Eqn
 $u_t = a^2 u_{xx}$

$$\text{B.C.s } \begin{cases} u_x(0, t) = 0 \\ u_x(L, t) = 0 \end{cases} \quad 0 \leq x \leq L$$

$$\text{I.C. } u(x, 0) = f(x)$$

(20%)

5. Evaluating the line integral of

$$\vec{F}(x, y, z) = -x\vec{i} + y\vec{j} - z\vec{k}$$

over the straight line segment from $(1, 1, 1)$ to $(-2, 1, 3)$

(20%)