

系別：機械與機電工程學系

科目：材 料 力 學

准帶項目請打「V」	
✓	計 算 機

本試題共 2 頁，4 大題

本試題雙面印製

1. In Fig. 1, a semi-circular rod ACB with circular cross section has the radius of r and flexural rigidity of EI . Its two ends are supported by hinges as shown. A vertical force P is applied at point C. Please determine: (a) the horizontal reaction force R_h at two supports; (b) the vertical deflection at point C. (25%)

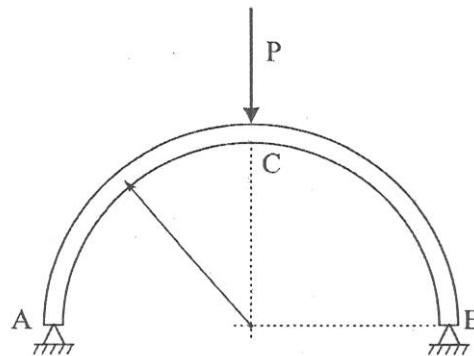


Fig. 1

2. In Fig. 2 a rectangular plate has the displacement $\bar{u}(x,y) = u(x,y)\hat{x} + v(x,y)\hat{y}$, where \hat{x} and \hat{y} are the unit vectors along x - and y -axes respectively. If the displacement components has the following forms:
- (a) $u = \alpha_1 + \beta_1 x, \quad v = \alpha_2 + \beta_2 y$
 - (b) $u = \alpha_3 + \beta_3 y, \quad v = \alpha_4 + \beta_4 x$
 - (c) $u = \alpha_5 x + \beta_5 y, \quad v = \alpha_6 x + \beta_6 y$

Determine strains $\epsilon_x, \epsilon_y, \epsilon_{xy}$, and plot the strain figures at point A for each cases. (25%)

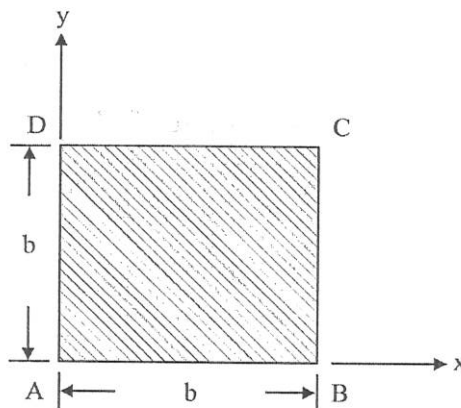


Fig. 2

准帶項目請打「V」	
✓	計 算 機

本試題共 2 頁，4 大題

3. A linearly elastic body, with the Young's modulus E and Poisson ratio ν , has the dimension $L \times h \times t$ as shown in Fig. 3. There are two rigid walls at the top and bottom of the body respectively, which limit the deformation of the body along y direction. A force P is applied in x direction, and therefore the body length is shortened $0.004L$. Please determine: (a) the force P ; (b) the stress q on the wall surfaces at the top and bottom of the elastic body; (c) the thickness increment Δt . (25%)

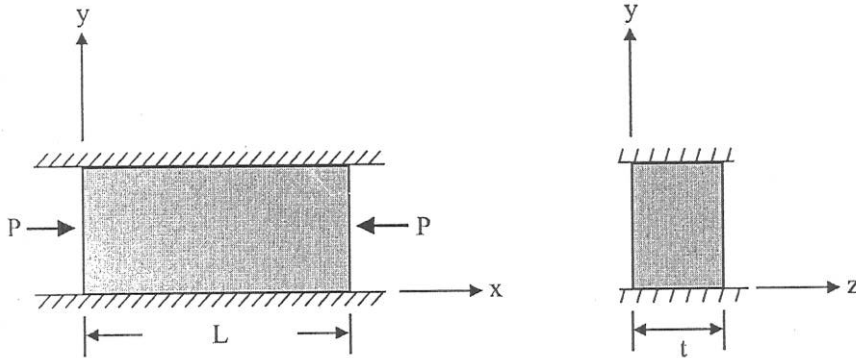


Fig. 3

4. A balloon has the diameter d of 10 cm and the thickness t of 0.1 mm as shown in Fig. 4. Assume its internal pressure p is 0.2 MPa. Please determine: (a) the membrane stress of the balloon; (b) the principal stress and the maximum shear stress of the outer surface of the balloon; (c) the principal stress and the maximum shear stress of the inner surface of the balloon. (25%)

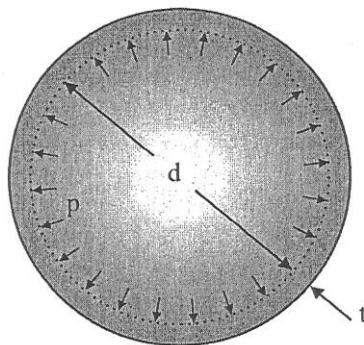


Fig. 4