

系別：工組二年級

科目：微 積 分

可否使用計算機			
可	✓	否	

本試題共 10 大題，一 頁

※ 1. 共 10 大題，每題 10 分。

2. 演算過程要寫清楚，直接寫答案不計分。

一、Find the following limits :

$$(1) \lim_{x \rightarrow 0^+} \frac{\frac{1}{2+x} - \frac{1}{2}}{2x} \quad (2) \lim_{x \rightarrow -2} \frac{\sqrt{x^2+5} - 3}{x^2+2x}$$

二、Find the integrals :

$$(1) \int e^x \cos x dx \quad (2) \int \frac{1}{2+2\sqrt{x}} dx$$

三、Let $f(x) = \begin{cases} 3x^2 - 1, & \text{if } x < 0 \\ cx + d, & \text{if } 0 \leq x \leq 1 \\ \sqrt{x+8}, & \text{if } x > 1 \end{cases}$, determine c and d so that f is continuous(連續) everywhere.

四、Find the absolute maximum and absolute minimum values of $f(x) = 6x^{4/3} - 3x^{1/3}$ on the closed interval $[-1, 1]$.

五、Given $x^3 + y^2x - 3 = 0$, Find dy/dx using implicit differentiation(隱微分).

六、 $f(x) = \frac{1}{1-2x}$, find $f^{(k)}(x)$.

七、Find the linear approximation $L(x)$ of $f(x) = \frac{1}{\sqrt{x+20}}$ at $a = 5$ and use it to approximate

$$\frac{1}{\sqrt{24.8}}.$$

八、Find the area(面積) of the region bounded by the parabola $y = x^2 - x - 6$ and the line $y = -4$.

九、(10%) Discuss(討論) if the series $\frac{1}{1 \cdot 3} + \frac{1}{2 \cdot 4} + \frac{1}{3 \cdot 5} + \frac{1}{4 \cdot 6} + \dots$ is convergent(是否收斂), find the sum if it is(若收斂求其和).

十、Find the interval of convergence(收斂範圍) of the power series $\sum_{n=0}^{\infty} \frac{2^n x^n}{3n+1}$.