

# 淡江大學八十七學年度日間部轉學生入學考試試題

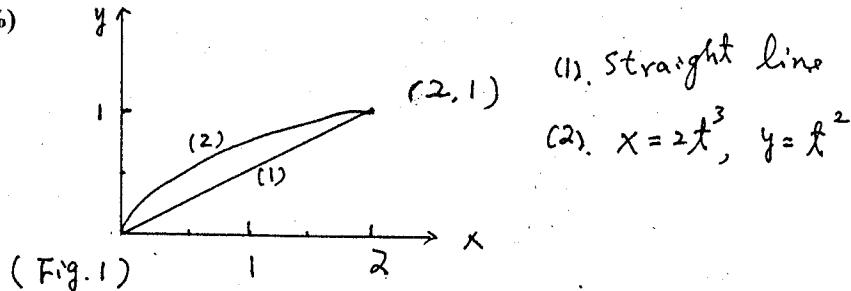
系別：物理系三年級

科目：應用數學

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1. Find  $\int_0^\infty t^n e^{-kt^2} dt$  for odd  $n, k > 0$ . (20%)

2. Given the force  $\mathbf{F} = xy\mathbf{i} - y^2\mathbf{j}$ , find the work done by  $\mathbf{F}$  along the paths indicated in Fig. 1 from  $(0,0)$  to  $(2,1)$ . (20%)



(1). Straight line

(2).  $x = 2t^3, y = t^2$

3. Solve differential equation  $x^2y' - 2xy = 1/x$ . (20%)

4. Find the eigenvalues and eigenvectors of the following matrices. (20%)

(a)  $\begin{pmatrix} 5 & -2 \\ -2 & 2 \end{pmatrix};$  (b)  $\begin{pmatrix} 1 & 3 & 0 \\ 3 & -2 & -1 \\ 0 & -1 & 1 \end{pmatrix}$

5. Find  $I = \int_0^{2\pi} \frac{d\theta}{5 + 4 \cos \theta}$ . (20%)